

Department of Electrical Engineering Program: B.E. (Electrical) Semester – Spring 2016

EL-322 Digital Signal Processing

Assignment – 2 Solution Marks: 10

Due Date: 22/04/2016 Handout Date: 18/04/2016

Question # 1:

Determine the inverse z-transform, using the method of partial fractions:

$$X(z) = \frac{1 - \frac{1}{2}z^{-1}}{1 + \frac{3}{4}z^{-1} + \frac{1}{8}z^{-2}}, \quad |z| > \frac{1}{2}$$

Solution:

$$\begin{split} X(z) &= \frac{1 - \frac{1}{2}z^{-1}}{1 + \frac{3}{4}z^{-1} + \frac{1}{8}z^{-2}}, \quad |z| > \frac{1}{2} \\ X(z) &= \frac{1 - \frac{1}{2}z^{-1}}{1 + \frac{3}{4}z^{-1} + \frac{1}{8}z^{-2}} = \frac{1 - \frac{1}{2}z^{-1}}{\left(1 + \frac{1}{4}z^{-1}\right)\left(1 + \frac{1}{2}z^{-1}\right)} \\ X(z) &= \frac{1 - \frac{1}{2}z^{-1}}{\left(1 + \frac{1}{4}z^{-1}\right)\left(1 + \frac{1}{2}z^{-1}\right)} = \frac{A}{1 + \frac{1}{4}z^{-1}} + \frac{B}{1 + \frac{1}{2}z^{-1}} \\ 1 - \frac{1}{2}z^{-1} &= A\left(1 + \frac{1}{2}z^{-1}\right) + B\left(1 + \frac{1}{4}z^{-1}\right) \\ X(z) &= \frac{A}{1 + \frac{1}{4}z^{-1}} + \frac{B}{1 + \frac{1}{2}z^{-1}} = \frac{-3}{1 + \frac{1}{4}z^{-1}} + \frac{4}{1 + \frac{1}{2}z^{-1}}, \quad |z| > \frac{1}{2} \\ x[n] &= \left[-3\left(-\frac{1}{4}\right)^n + 4\left(-\frac{1}{4}\right)^n\right]u[n] \end{split}$$

Question # 2:

The continuous time signal

$$x_c(t) = \cos(4000\pi t)$$

Is sampled with a sampling period T to obtain a discrete-time signal:

$$x[n] = \cos\left(\frac{\pi n}{3}\right)$$

- a) Determine a choice for T consistent with this information.
- b) Is your choice for T in part (a) unique? If so, explain why. If not, specify another choice of T consistent with the information given.

Solution:

a) Since $x[n] = x_c(nT)$,

$$\frac{\pi n}{3} = 4000\pi nT$$
$$T = \frac{1}{12000}$$

b) No our choice for T is not unique. For example, since (π) (7π)

$$\cos\left(\frac{\pi}{3}n\right) = \cos\left(\frac{7\pi}{3}n\right)$$

T can be 7/12000.

Good Luck