



# Signal & Systems

## Lecture #1

6<sup>th</sup> March 18



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# Course Assessment

- + Total assessment 100 %
  - + Midterm : 30%
  - + Final Exam : 50%
  - + Internal Evaluation : 20%
- + Internal Evaluation 20%
  - + Quizzes : 10%
  - + Assignment : 10%

# Internal Evaluation Details

+ Total Quizzes 5

Best of 4 Quizzes

+ Semester Project will be conducted in the form of groups.

+ Evaluation will be equal to 1 quiz and 1 assignment

Total 5 Quizzes

Total Assignments 5

Best of 4 Assignments

Total 5 Assignments

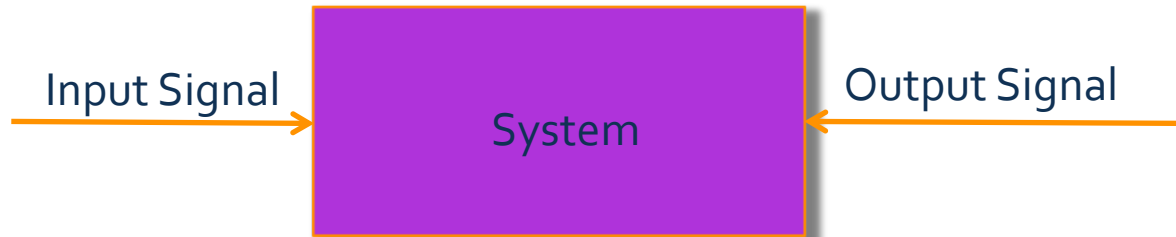
# Course Book

- + Signal & Systems, By Alan V. Oppenheim, Alan S. Willsky with S.Hamid Nawab



# Introduction

# What is a Signal?



- + If a function represents a physical quantity or variable containing information about the behavior and nature of the phenomenon.
- + Signals are functions of one or more variables.

# Examples of Signals

- + Examples of signals include:
  - + **A Voltage signal:** voltage across two points varying as a function of time.
  - + **A photograph:** color and intensity as a function of 2-dimensional space.
  - + **A Video Signal:** color and intensity as a function of 2-dimensional space and time.



# What is a System?

- + Systems are operator that accept a given signal (the input) and produces a new signal (the output).
- + Systems respond to an input signal by producing an output signal.

# Examples of Systems

- + Examples of system includes:
  - + **An Oscilloscope:** takes in a voltage signal, outputs a 2-dimensional image characteristic of the voltage signal.
  - + **A computer monitor:** inputs voltage pulses from the CPU and outputs a time varying display.
  - + **A capacitance:** terminal voltage signal may be looked at as the input, current signal as the output.

# Classification of Signals

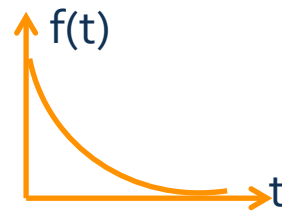


# Classification

- + Two main broad classification of signals are:
  - + Continuous time signal
  - + Discrete time signal

# Continuous Time Signals

- + It is an infinite and uncountable set of numbers.
- + There are infinite possible values from the time  $t$  and instantaneous amplitude  $x(t)$  between start and end point.
- + If a signal at all values of  $t$  is a continuous variable:

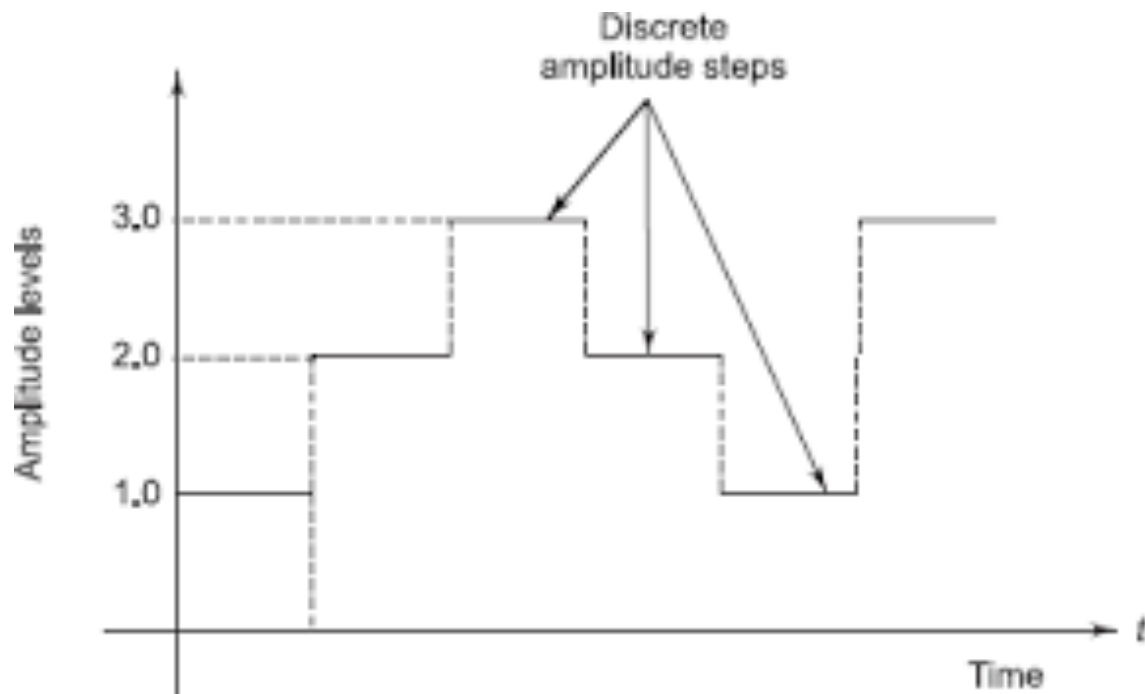


Exponential  
Function

- + This signal is continuous in time as well as in amplitude.
  - + Another example is Sinusoidal Signal.

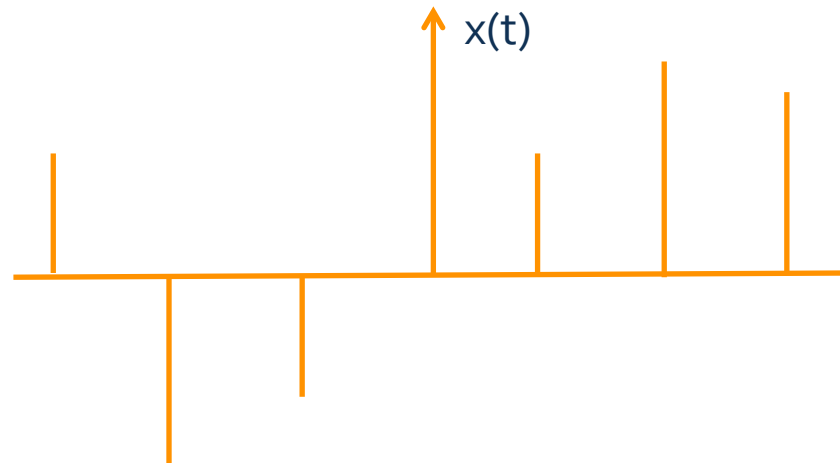
# Continuous Time Signals (cont.)

- + The signal shown below is continuous in time but discrete in amplitude.



# Discrete Time Signals

- + The number of elements in the set as well as possible values of each element is finite and countable.
- + It can be represented with computer bits and stored on a digital storage medium.



# Basic Operations





# Elementary Operations on Signals

- + There are several basic operation by which new signals are formed from given signals:
  - + Amplitude Scale:  $y(t) = ax(t)$ , where a is a real (or possibly complex) constant.
  - + Amplitude Shift:  $y(t) = x(t) + b$ , where b is a real = (or possibly complex) constant
  - + Addition:  $y(t) = x(t) + z(t)$
  - + Multiplication:  $y(t) = x(t)z(t)$

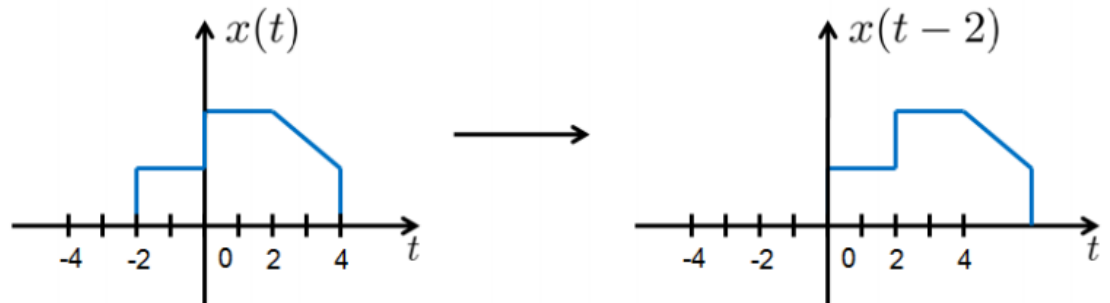
# Time Shift

- + For any  $t_0 \in \mathbb{R}$  and  $n_0 \in \mathbb{Z}$  time shift is an operation defined as:

$$x(t) \rightarrow x(t - t_0)$$

$$x[n] \rightarrow x[n - n_0]$$

- + If  $t_0 > 0$ , the time shift is known as “delay”.
- + If  $t_0 < 0$ , the time shift is known as “advance”.
- + For example:



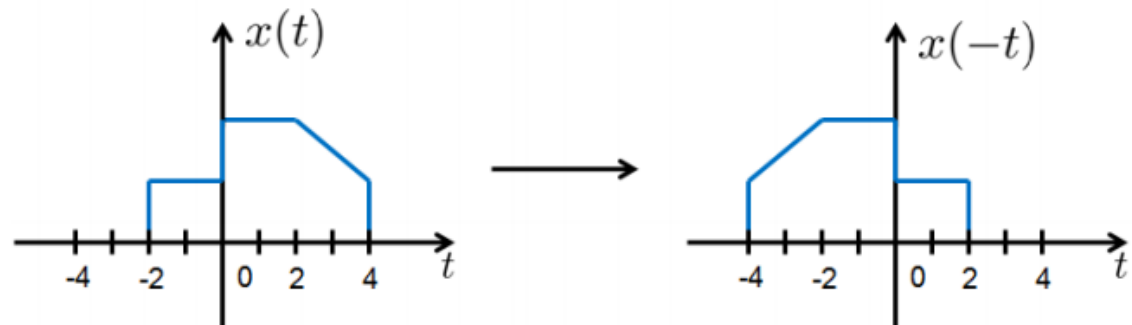
# Time Reversal

- + Time reversal is defined as:

$$x(t) \rightarrow x(-t)$$

$$x[n] \rightarrow x[-n]$$

- + Which can be interpreted as the “flip over the y-axis”.
- + For example:

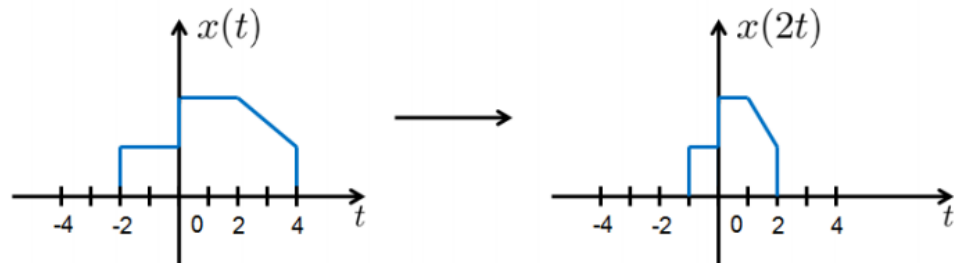


# Time Scaling

- + Time scaling is the operation where the time variable  $t$  is multiplied by a constant  $a$ :

$$x(t) \rightarrow x(at), \quad a > 0$$

- + If  $a > 1$ , the time scale of the resultant signal is “decimated” (speed up).
- + If  $0 < a < 1$ , the time scale of the resultant signal is “expanded” (slowed down).
- + For example:



# Combination of Operations

- + Linear operation in time on a signal  $x(t)$  can be expressed as:

$$y(t) = x(at - b), \quad a, b \in R$$

- + There are two methods to describe the output signal:

- + Method A: "shift, then scale"

- + Define  $v(t) = x(t-b)$

- + Define  $y(t) = v(at) = x(at-b)$

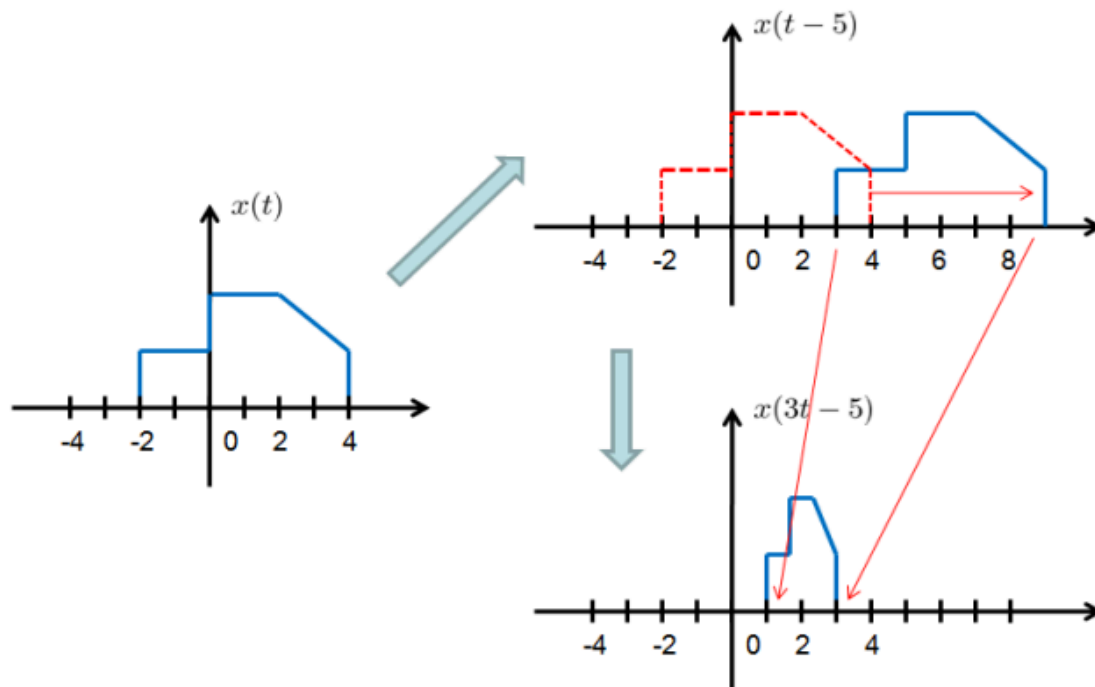
- + Method B: "Scale, then shift"

- + Define  $v(t) = x(at)$

- + Define  $y(t) = v(t-b/a) = x(at-b)$

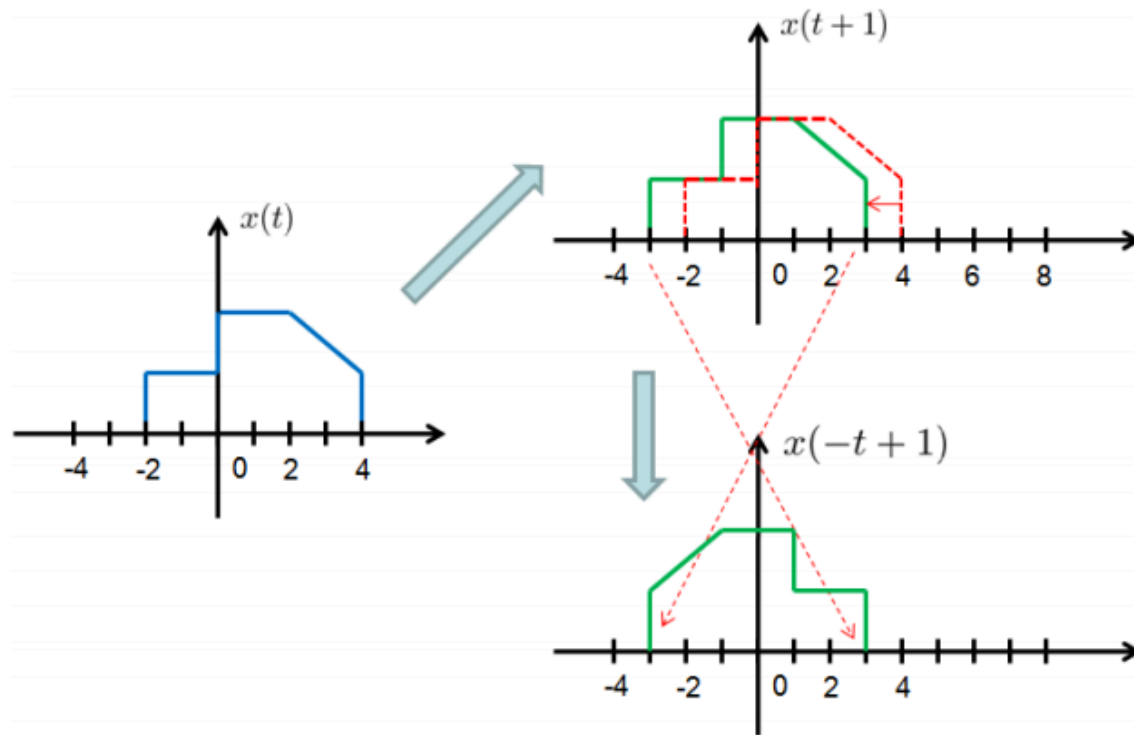
# Combination of Operations (cont.)

+ Example 1:



# Combination of Operations (cont.)

+ Example 2:



# Example #1

- + Given the signal  $x(t)$  as shown below:



- + (a): Draw the signal  $x(t+1)$
- + (b): Draw the signal  $x(-t+1)$  obtained by a time shift and a time reversal.
- + (c): Draw the time scaled signal  $x(3/2t)$
- + (d): Draw the signal  $x(3/2t+1)$  obtained by a time shift and scaling.

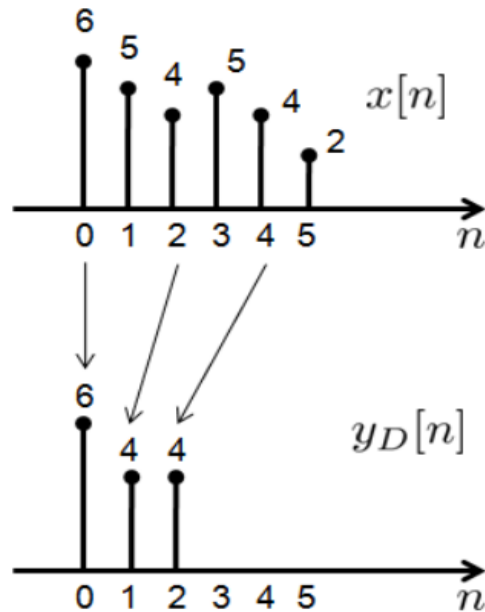


# Decimation & Expansion



# Decimation

- + Decimation is defined as:  $y_D[n] = x[Mn]$
- + For some integers M. M is called the decimation factor.
- + When M=2.



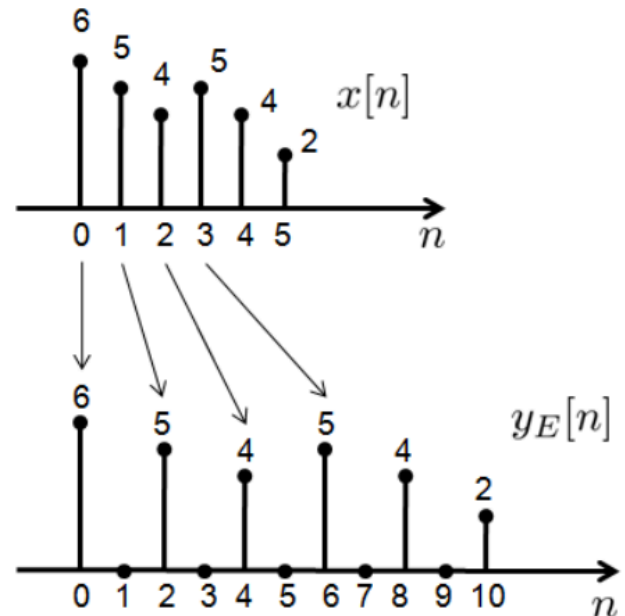
# Expansion

+ Expansion is defined as:

$$y_E[n] = \begin{cases} x\left[\frac{n}{L}\right], & n = \text{integer multiple of } L \\ 0, & \text{otherwise} \end{cases}$$

❖ L is called the expansion factor.

❖ When L=2.



# Classification of Signals



# Periodic vs Aperiodic

- + Definition-1: A continuous time signal  $x(t)$  is periodic if there is a constant  $T > 0$  such that:

$$x(t) = x(t + T), \quad \text{for all } t \in \mathbb{R}$$

- + Definition-2: A discrete time signal  $x[n]$  is periodic if there is an integer constant  $N > 0$  such that:

$$x[n] = x[n + N], \quad \text{for all } n \in \mathbb{Z}$$

- + Signals do not satisfy the periodicity conditions are called aperiodic signals.
- +  $T_0$  is called the fundamental period of  $x(t)$  if it is the smallest value of  $T > 0$  satisfying the periodicity condition. The number  $\omega_0 = \frac{2\pi}{T_0}$  is called the fundamental frequency of  $x(t)$ .

# Periodic vs Aperiodic (cont.)

- +  $N_0$  is called the fundamental period of  $x[n]$  if it is smallest value of  $N > 0$  where  $N \in \mathbb{Z}$  satisfying the periodicity condition. The number  $\frac{\Omega_0}{2\pi} = \frac{m}{N}$  is called the fundamental frequency of  $x[n]$ .

## Example #2

+ Determine the fundamental period of the following signals:

$$(a): e^{j3\pi t/5}$$

$$(b): e^{j3\pi n/5}$$

# Even & Odd Signals

- + An even signal is any signal  $f$  such that  $f(t) = f(-t)$ .
- + A signal  $x(t)$  or  $x[n]$  is referred to as an even signal if it is identical to its time-reversed counterpart, i.e., with its reflection about the origin.
- + An odd signal on the other hand is a signal  $f$  such that  $f(t) = -f(-t)$ .
- + Any signal can be written as a combination of an even and odd signal, i.e., every signal has an odd-even decomposition.

$$f(t) = \frac{1}{2}(f(t) + f(-t)) + \frac{1}{2}(f(t) - f(-t))$$



## Even & Odd Signals (cont.)

- ❖ The all-zero signal is both even and odd. Any other signal cannot be both even and odd, but may be neither.

Thank You

